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Spatio-temporal small-scale features of force-free field-aligned currents in space plasmas

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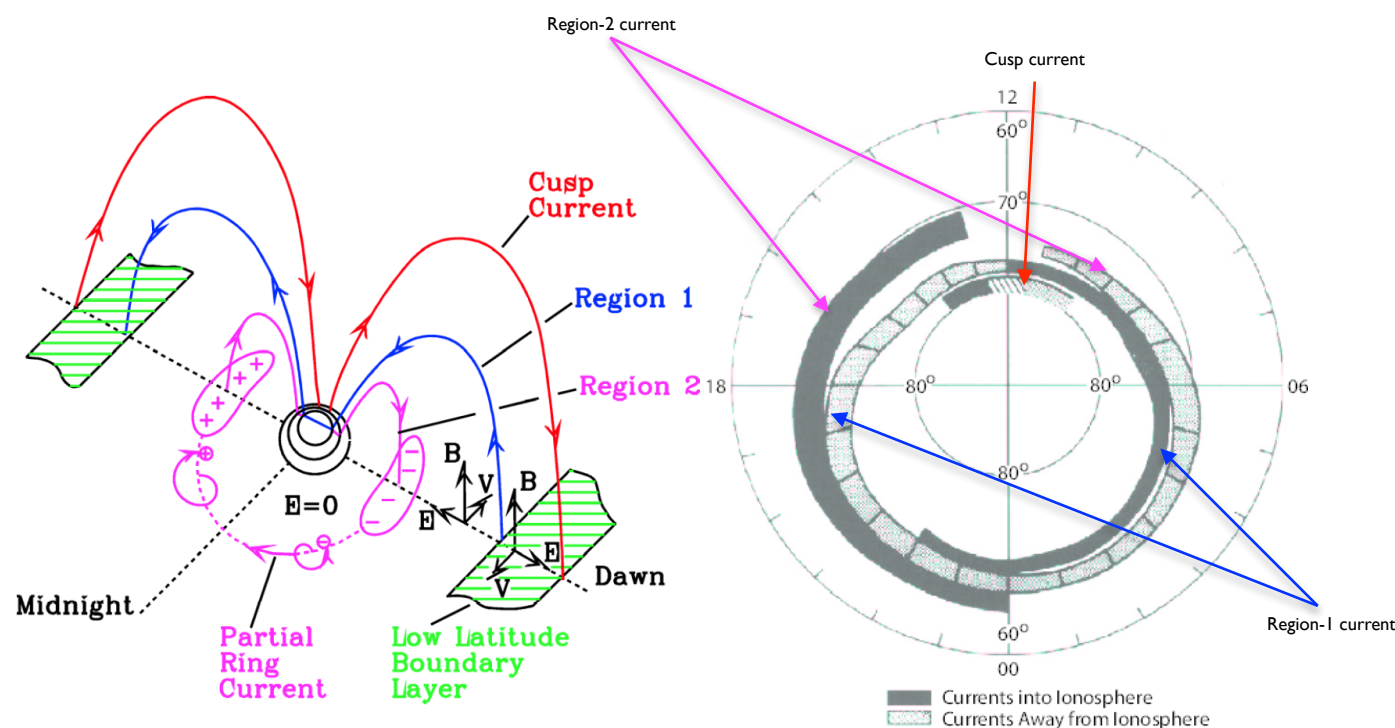


Introduction

Field-Aligned-Currents (FACs) play a very important role in several processes taking place in the circumterrestrial environment (magnetosphere, ionosphere,...)

FACs were originally postulated by Birkeland (*Birkeland*, 1908) and detected for the first time sixty years later by spacecraft observations of localized magnetic fluctuations (*Zmuda et al.*, 1966; *Cummings and Dessler*, 1967).

In the polar ionosphere, the *pattern of FACs* consists of *two current belts* (*Region-1* and *Region-2*) that flow upward and downward along the magnetic field lines according to latitude and magnetic local time.



from R. McPherron, AGU FM 2005

from Iijima and Potemra, 1976

FACs play a crucial role in *energy and momentum transfer among different circumterrestrial regions*: the solar wind the magnetosphere the ionosphere and thermosphere.

The knowledge of their structure is of *uppermost importance to understand how energy deposition processes*.



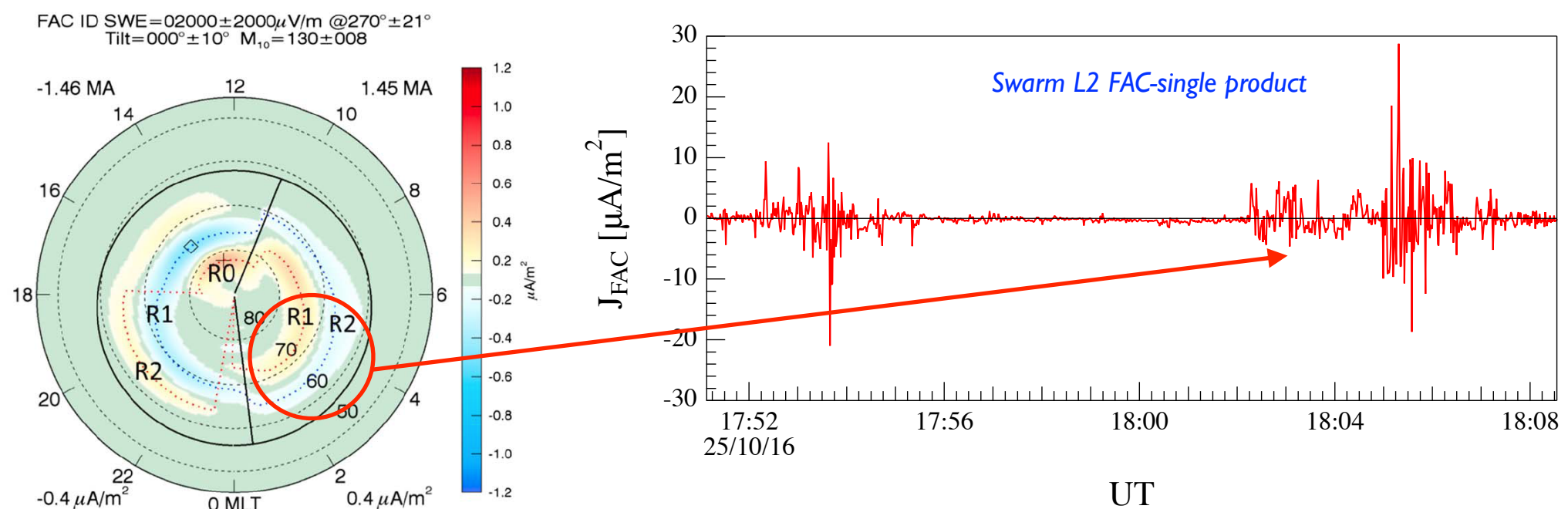
Introduction

Although significant progresses have been achieved, some scientific questions still need to be answered.

An interesting point is the *characterization of the FAC structure on small-spatial scales* and their link with *turbulence phenomena*.

Surveys (Neubert and Christiansen, 2003) have shown that *small-scale FACs* can be found throughout the *auroral oval and the pre-noon cusp region*.

These currents (typical *widths* of a *few hundred meters*) are very intense reaching *several hundreds $\mu\text{A}/\text{m}^2$* (Lühr et al., 1994; Stasiewicz and Potemra, 1998).





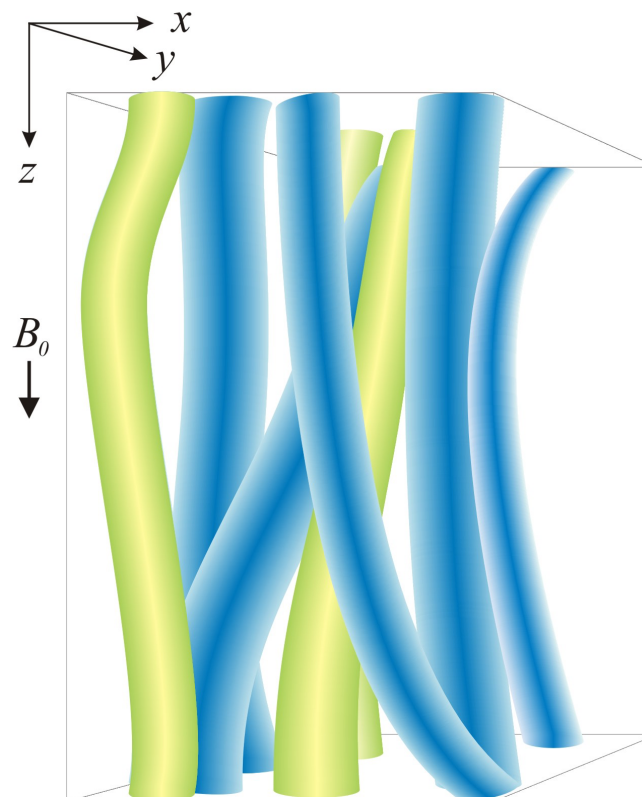
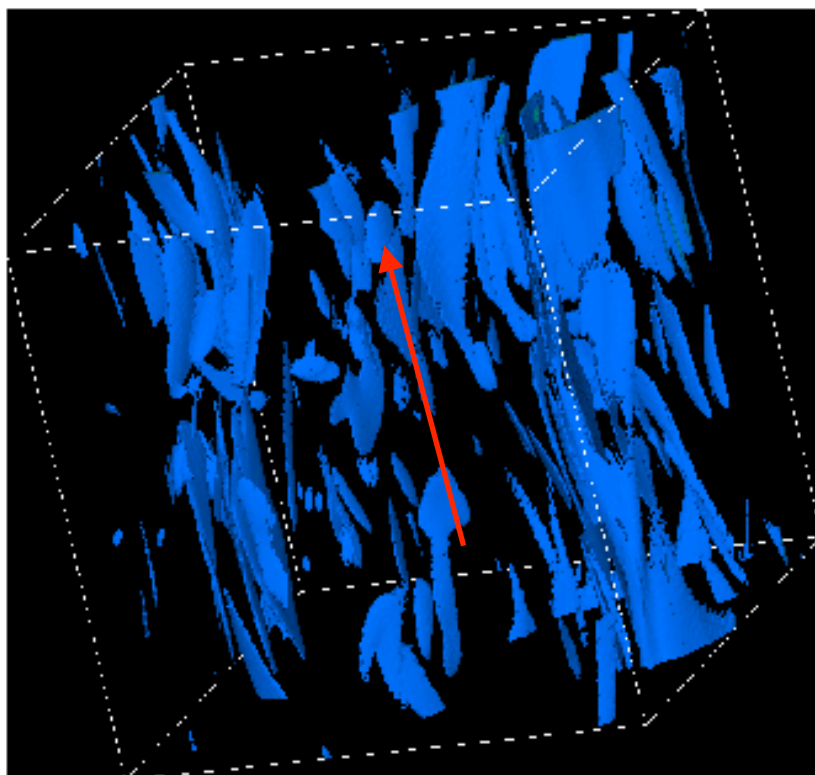
Theoretical framework

Small-scale FACs are *randomly oriented* due to their *possible filamentary structure* and their origin might be linked with the occurrence of *turbulence*.

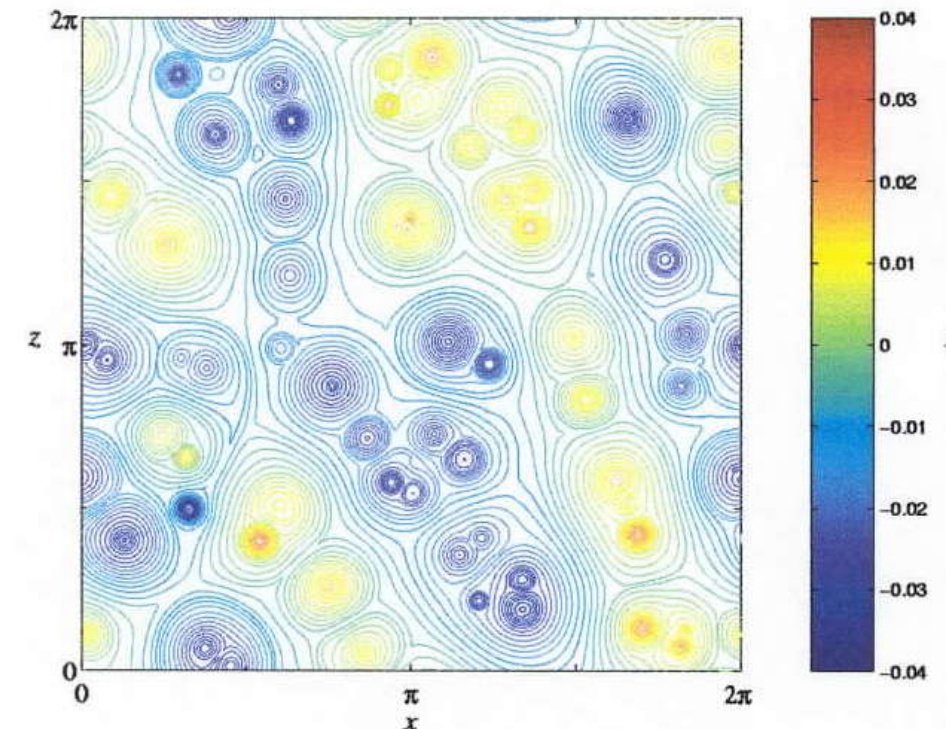
Turbulence, indeed, plays a crucial role in generating *multiscale coherent structures in the form of flux tubes*.

$B \neq 0 \Rightarrow$ ribbons

from Biskamp & Nüller, 2000



from Wu and Chang, GRL, 2000



Theoretical framework

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Turbulence, indeed, plays a crucial role in generating *multiscale coherent structures in the form of flux tubes*.

$$\mathbf{B} = \mathbf{e}_z \times \nabla \psi + B_0 \mathbf{e}_z \rightarrow \mathbf{B} = (\delta B_x, \delta B_y, B_0)$$

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$$\mathbf{J} \times \mathbf{B} \sim 0$$

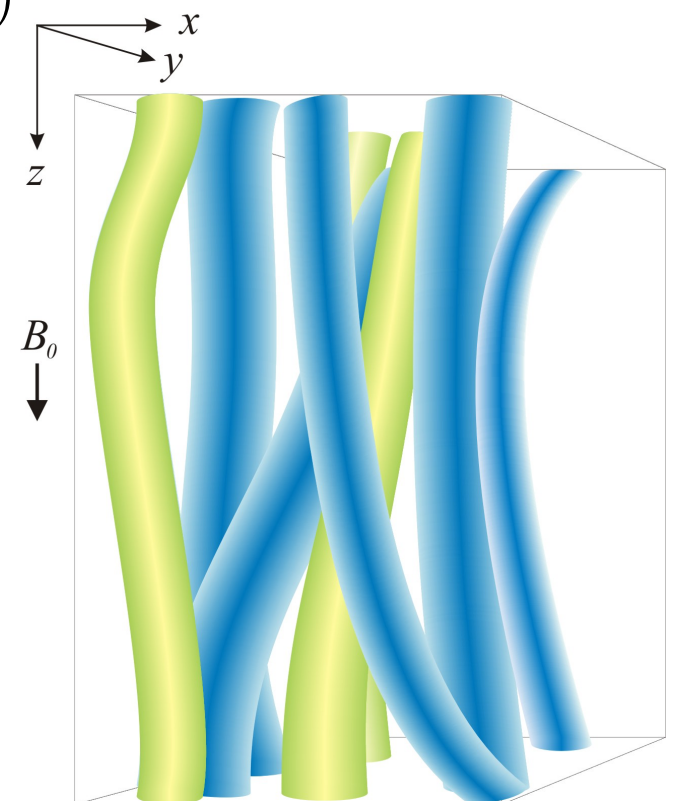
$$\nabla \cdot \mathbf{J} \sim 0$$

$$\mathbf{B} \cdot \nabla J_z = 0$$

$$\nabla \cdot \mathbf{B} = 0$$

$$B_0 \frac{\partial J_z}{\partial z} = - \left(\delta B_x \frac{\partial}{\partial x} + \delta B_y \frac{\partial}{\partial y} \right) J_z + \dots$$

$$(\delta B_x, \delta B_y) = \left(\frac{\partial \psi}{\partial y}, -\frac{\partial \psi}{\partial x} \right)$$

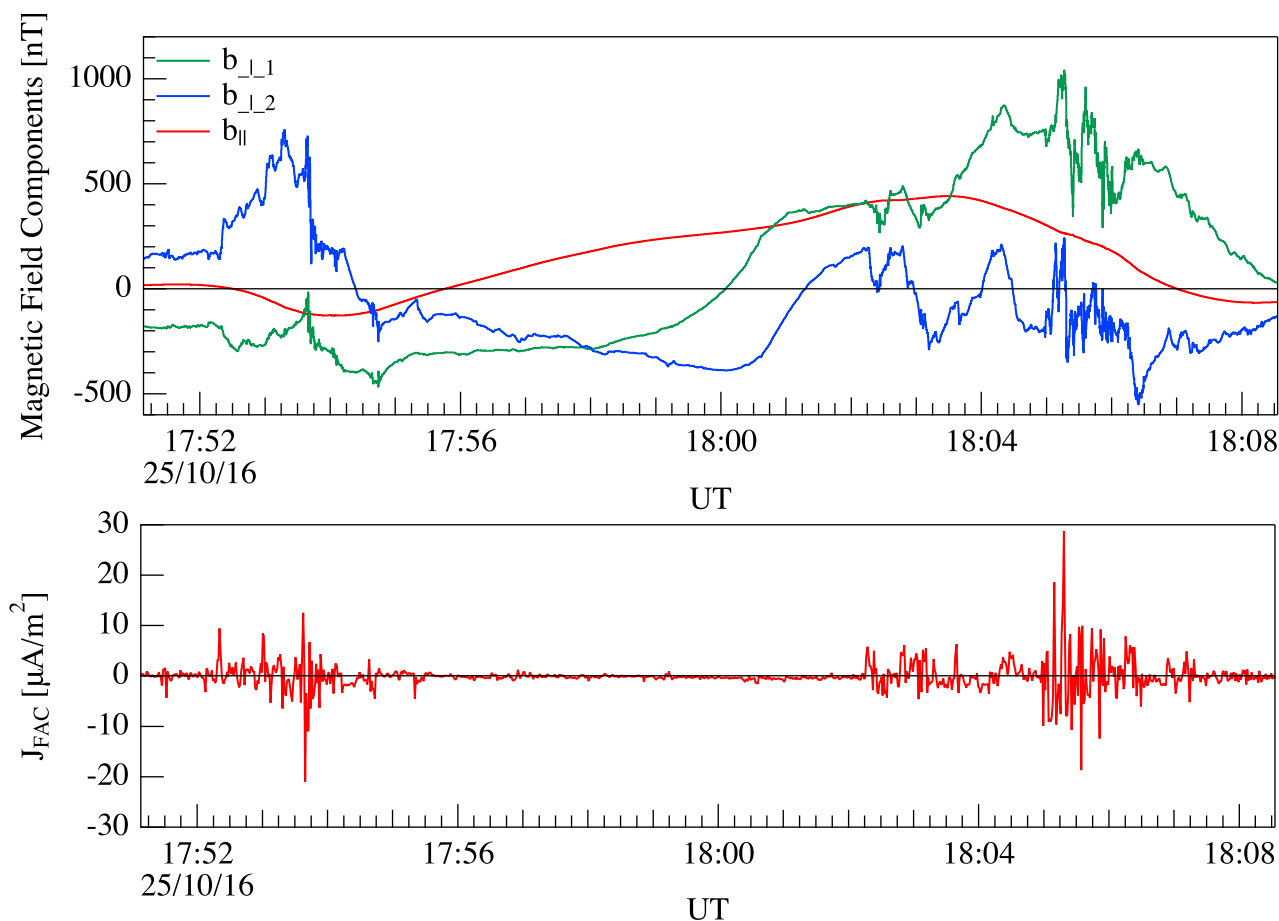




Data description

This study is based on *in-situ* observations of FACs via magnetic field measurements by *ESA-Swarm satellites*, *Swarm A* and *C*.

We selected two days characterized by a different geomagnetic activity level: *October 21*, and *October 25, 2016*, during which the average *AE-index value* is *160 nT* and *660 nT*, respectively.

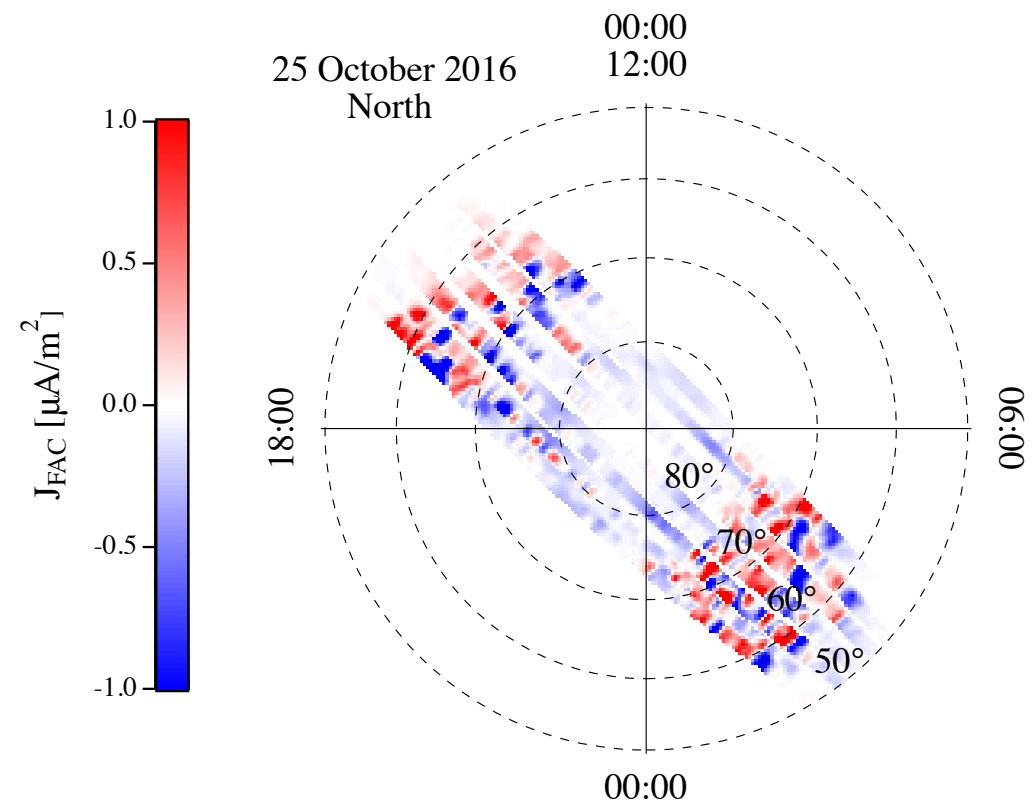
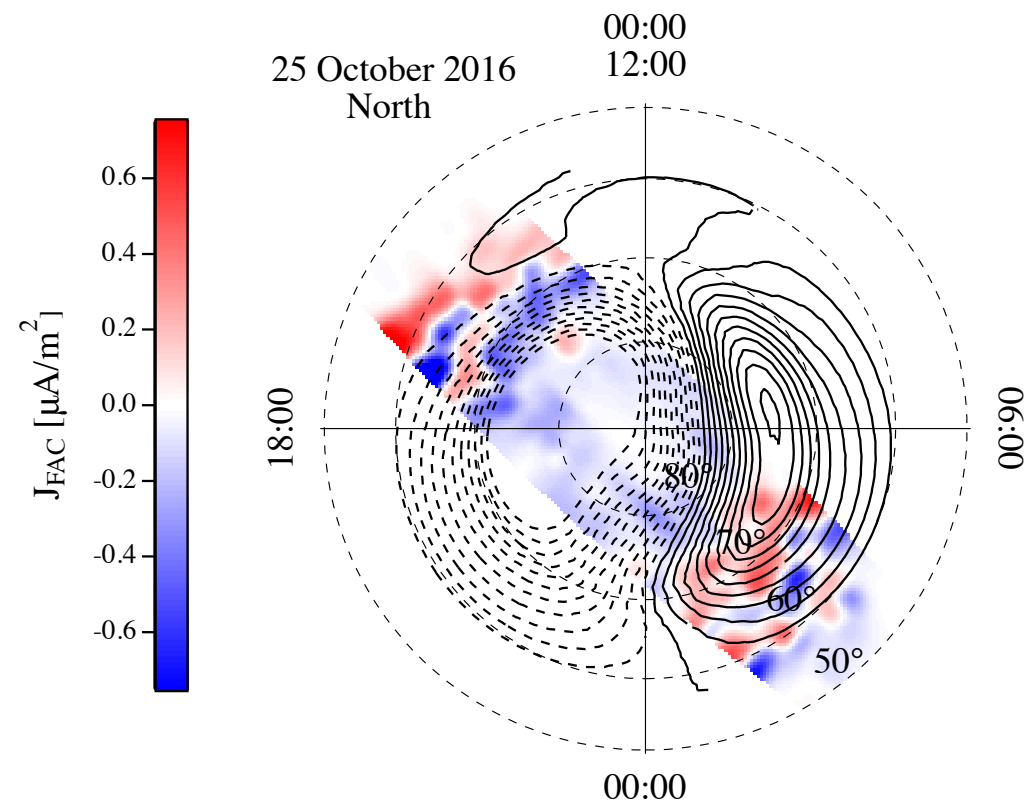
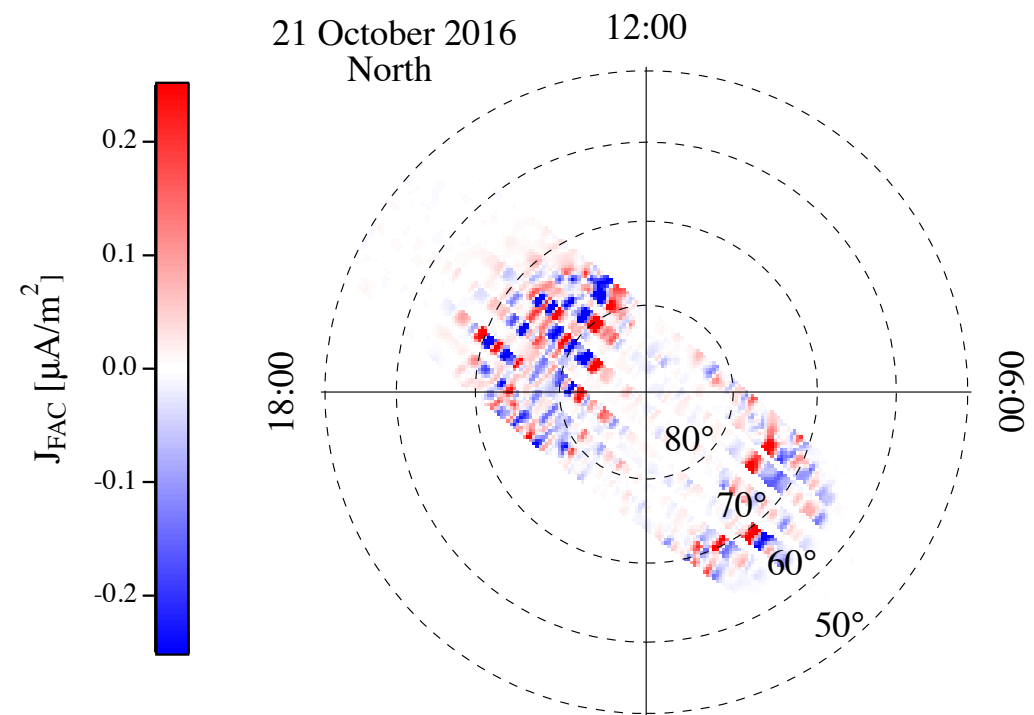
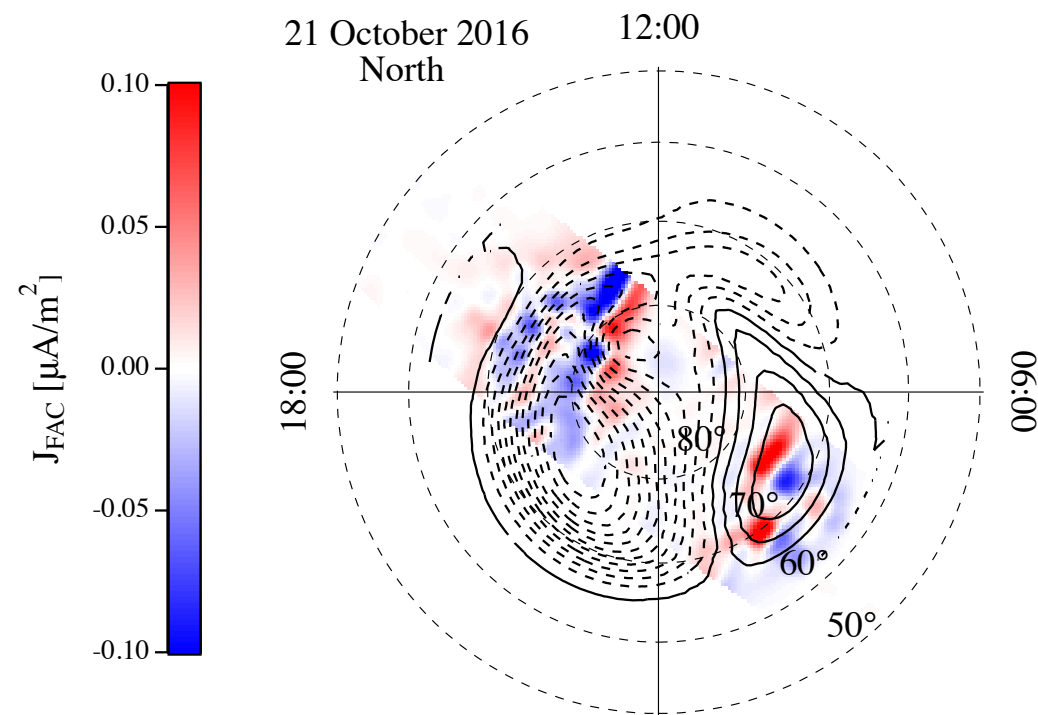


FAC density data, used in this analysis, are the *Swarm Level-2 (L2-FAC) single-spacecraft product* (Ritter et al., 2013), calculated from the spatial gradients of the magnetic field observed along the direction defined by the spacecraft orbit track (ftp://swarm-diss.eo.esa.int/FACATMS_2F file type).

Temporal resolution is 1 s.



Data description





Analysis Method: Sign-Singularity Measure

The properties of many physical processes can be described by *multifractal probability measures*. In contrast with *positive measures*, a *signed measure* can be useful to describe and to characterize *random fields which oscillate in sign*.

Ott et al. (1992) introduced a *scaling exponent κ* (the *cancellation exponent*) to characterize the *sign-singularity* of a signed measure.

Let $f(t)$ be a signal with zero mean, over a finite interval T . Consider a partition of size ϵ covering the interval T . On each subset T_i it is possible to define a *signed measure, $\mu_\epsilon(T_i)$* ,

$$\mu_\epsilon(T_i) = \int_{T_i} f(t) dt$$

By introducing a *partition function $\chi(\epsilon)$*

$$\chi(\epsilon) = \sum_i | \mu_\epsilon(T_i) |$$

the *cancellation exponent κ* can be defined as

$$\kappa = - \lim_{\epsilon \rightarrow 0} \frac{\ln \chi(\epsilon)}{\ln \epsilon}$$



Analysis Method: Sign-Singularity Measure

For a *positive measure* $\kappa = 0$, being trivially $\chi(\varepsilon) = \text{const} \forall \varepsilon$. Conversely, for *non-positive sign-singular measures* $\kappa > 0$ at least on scales larger than a cutoff below which the measure is regular and smooth with a well defined sign.

For 1D signals the *cancellation exponent* κ is generally in the *range* $[0,1]$, with $\kappa=1/2$ for *Brownian motions* and *Markovian stochastic* signals, and $\kappa=1$ for *nondifferentiable signals* (Bertozzi and Chhabra, 1994; Vainshtein et al., 1994).

As clearly shown in some specific study of both *fluid and MHD turbulence* (Bertozzi and Chhabra, 1994; Vainshstein et al., 1994; Carbone and Bruno, 1996) the value of the *cancellation exponent* can be linked to other *scaling features*: the *structure functions*.

For instance, for the Kolmogorov scaling (Frisch, 1995) the *first order structure function* of the fluid velocity at the *scale* ε is related to the *partition function* $\chi(\varepsilon)$ by the expression,

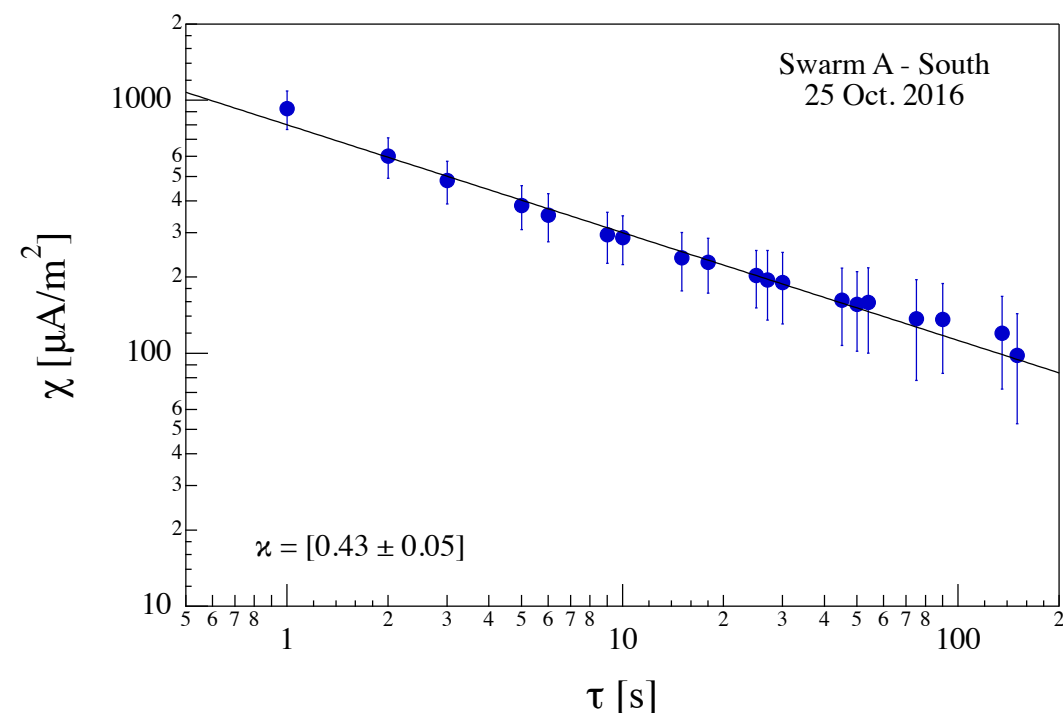
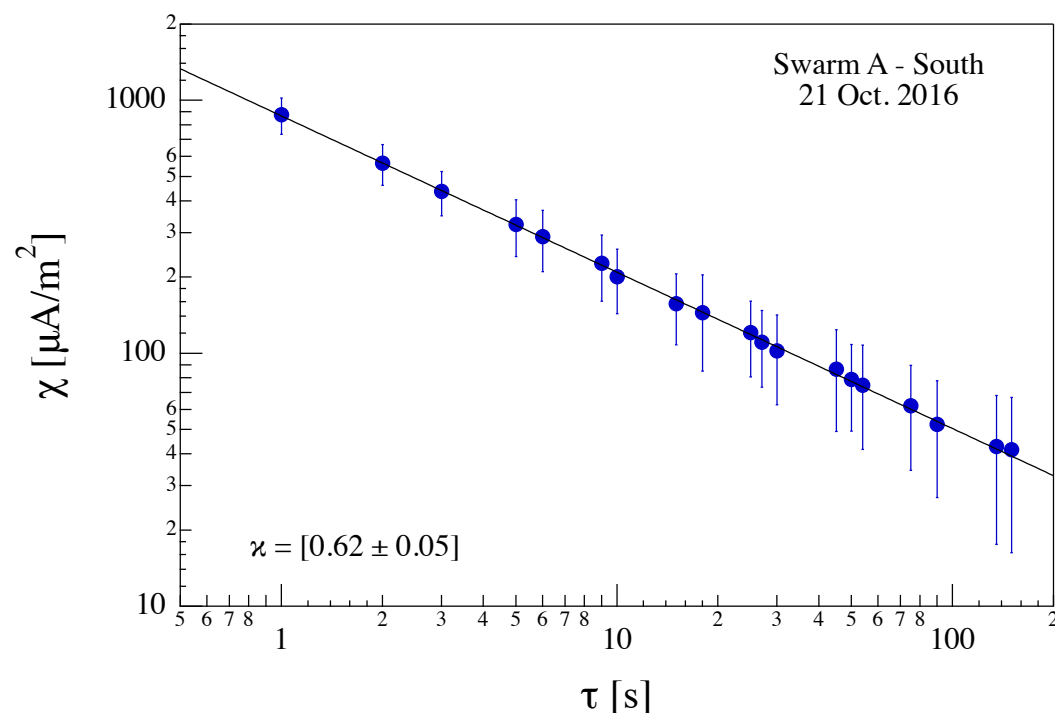
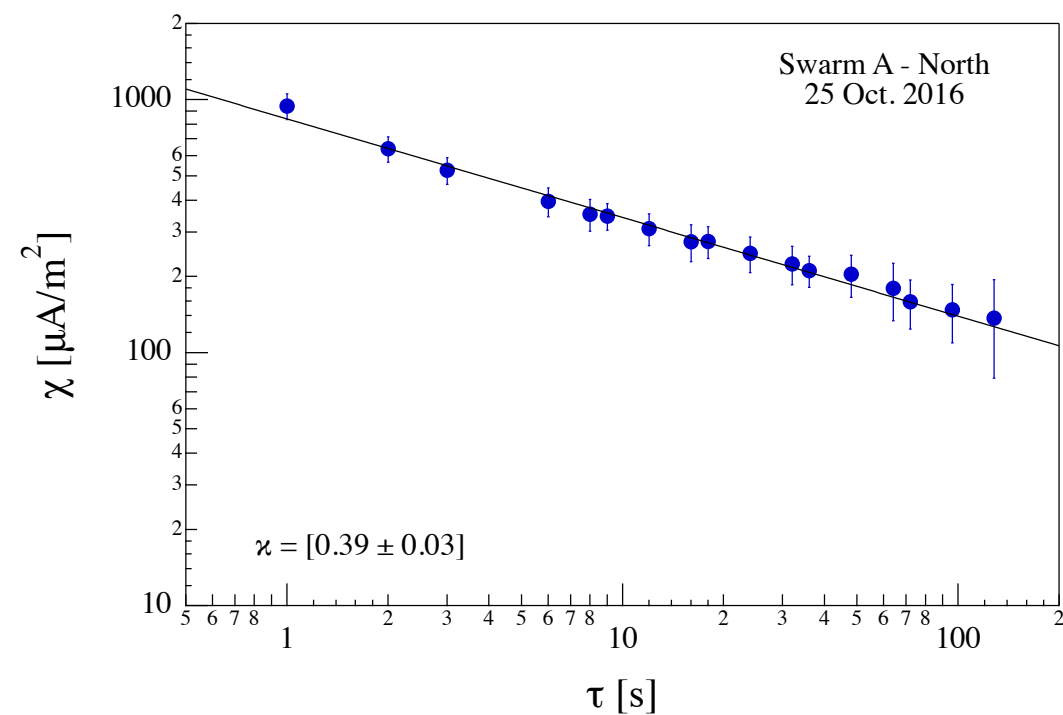
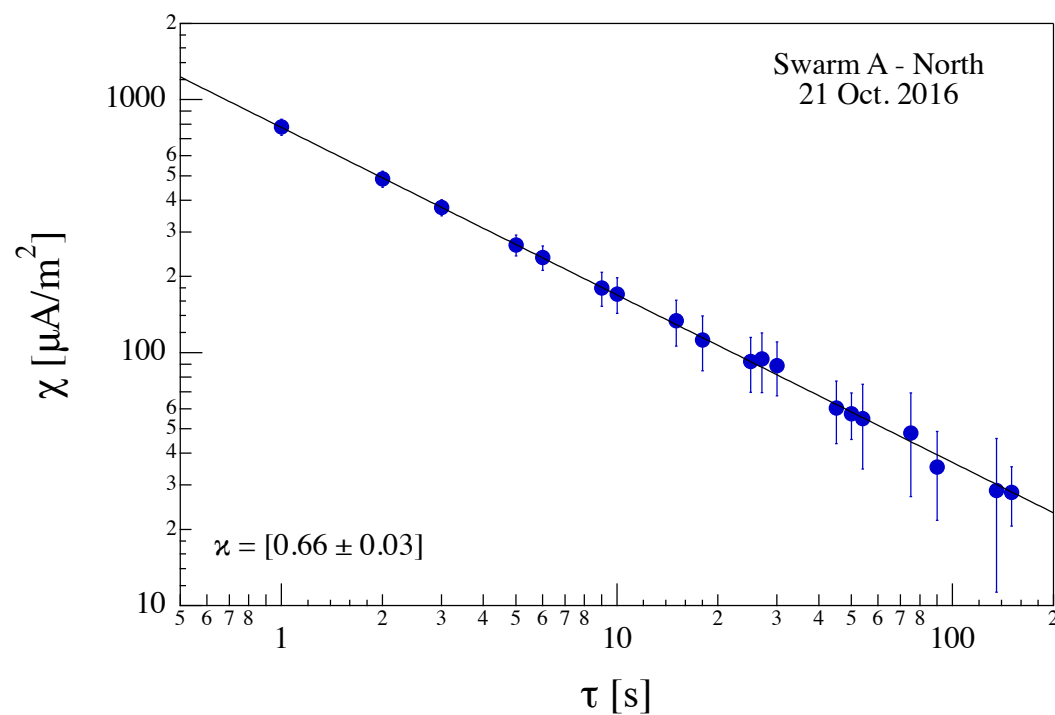
$$\langle |v_{||}(r + \varepsilon) - v_{||}(r)| \rangle \sim \varepsilon \chi(\varepsilon)$$

$$\kappa = 1 - \gamma(1)$$



Results

$$\mu_{\tau}(\Omega_i) = \sum_{t_k \in \Omega_i} j_{FAC}(t_k) \rightarrow \chi(\tau) = \sum_i | \mu_{\tau}(\Omega_i) |$$





Results

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Cancellation Exponent κ

21 Oct 2016	Swarm A	Swarm C
North	0.66 ± 0.03	0.67 ± 0.03
South	0.62 ± 0.05	0.62 ± 0.05

25 Oct 2016	Swarm A	Swarm C
North	0.39 ± 0.03	0.38 ± 0.03
South	0.43 ± 0.05	0.43 ± 0.05



Conclusions

The results of our analysis returns:

- the FAC fluctuations show *non-trivial sign-singularity*;
- the observed *scaling features are non-trivial* and *depend on the geomagnetic disturbance level*: the *cancellation exponent κ decreases for increasing geomagnetic activity* (AE-index);

$$\langle AE - index \rangle = 160 \text{ nT} \longrightarrow \langle \kappa \rangle = [0.64 \pm 0.04] \quad (\gamma(1) = 0.36)$$

$$\langle AE - index \rangle = 660 \text{ nT} \longrightarrow \langle \kappa \rangle = [0.41 \pm 0.04] \quad (\gamma(1) = 0.59)$$

intermittency

- the cancellation exponent values point toward an *intermittent turbulent* character of the observed current fluctuations.

These preliminary results support the *filamentary nature (strong inhomogeneity)* of the FACs in the polar ionosphere. However, more work is necessary to put all the emerging scenario in a theoretical framework.



Acknowledgements

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